

Algorithm Theoretical Basis Document

Aquarius Salinity Retrieval Algorithm: Final Pre-Launch Version

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1 Introduction

This document provides the theoretical basis for the Aquarius salinity retrieval algorithm. The inputs to the algorithm are the Aquarius antenna temperature (T_A) measurements along with a number of NCEP operational products and pre-computed tables of space radiation coming from the galaxy and sun. The output is sea-surface salinity and many intermediate variables required for the salinity calculation. This revision of the ATBD is intended to be the final pre-launch version.

The ATBD is organized into two main sections. The Forward Model Section describes how the Aquarius antenna temperature is calculated given the following information:

1. Footprint location: time, latitude, and longitude
2. Pointing angles: Earth incidence and azimuth angles; sun and moon pointing vectors
3. Antenna pattern
4. NCEP operational fields: surface temperature and vector wind, atmospheric profiles (pressure, temperature, humidity, liquid water), sea ice
5. Solar flux values from radio astronomy observations
6. Pre-computed tables giving the T_A contribution of the galaxy and sun (moon contribution is computed from an analytic expression)

The Retrieval Algorithm Section describes how the various components of the forward model are used to estimate salinity given the Aquarius T_A measurement. The algorithm is essentially a subtraction process in which the unwanted sources of radiation (galaxy, sun, moon, and Earth's atmosphere) are removed from the T_A measurement in order to obtain just the Earth's surface emission term. A simple regression is then used to estimate salinity from the surface emission.

2 The Forward Model

The forward model gives the Aquarius antenna temperature in terms of the antenna pattern G convolved with the surrounding brightness temperatures (T_B) 4π -steradian field. The convolution of G with T_B is called the antenna temperature equation. The field of surrounding brightness temperatures is partitioned into a space segment and an Earth segment.

2.1 The Antenna Temperature Equation

In this subsection, we work in terms of the classical, rather than the modified, Stokes parameters. The measurement vector $\mathbf{T}_{A,mea}$, which is called the antenna temperature vector, is then defined as:

$$\mathbf{T}_{\mathbf{A},mea} \equiv \begin{bmatrix} T_{A1,mea} \\ T_{A2,mea} \\ T_{A3,mea} \\ T_{A4,mea} \end{bmatrix} = \begin{bmatrix} T_{Amea,V} + T_{Amea,H} \\ T_{Amea,V} - T_{Amea,H} \\ T_{Amea,+45} - T_{Amea,-45} \\ T_{Amea,left} - T_{Amea,right} \end{bmatrix} \quad (1)$$

where $T_{Amea,V}$, $T_{Amea,H}$, $T_{Amea,+45}$, $T_{Amea,-45}$, $T_{Amea,left}$, and $T_{Amea,right}$ are the v-pol, h-pol, plus 45°, minus 45°, left circular, and right circular polarization measurements. Aquarius will only measure $T_{Amea,V}$, $T_{Amea,H}$, $T_{Amea,+45}$, and $T_{Amea,-45}$, but the full Stokes formulation is included here for completeness. Likewise, brightness temperatures are defined as

$$\mathbf{T}_{\mathbf{B}} \equiv \begin{bmatrix} T_{B1} \\ T_{B2} \\ T_{B3} \\ T_{B4} \end{bmatrix} = \begin{bmatrix} T_{B,V} + T_{B,H} \\ T_{B,V} - T_{B,H} \\ T_{B,+45} - T_{B,-45} \\ T_{B,left} - T_{B,right} \end{bmatrix} \quad (2)$$

The measurements represent an integration over the entire 4π steradians surrounding the antenna. We divide this integration into 2 components: the Earth field of view and the space field of view.

$$\mathbf{T}_{\mathbf{A},mea} = \mathbf{T}_{\mathbf{A},earth} + \mathbf{T}_{\mathbf{A},space} \quad (3)$$

$$\mathbf{T}_{\mathbf{A},earth} = \frac{1}{4\pi} \int_{Earth} \mathbf{G}(\mathbf{b}) \Psi(\phi) \mathbf{T}_{\mathbf{B},toa} \frac{\partial \Omega}{\partial A} dA \quad (4)$$

$$\mathbf{T}_{\mathbf{A},space} = \frac{1}{4\pi} \int_{Space} \mathbf{G}(\mathbf{b}) \mathbf{T}_{\mathbf{B},space} d\Omega \quad (5)$$

The first integral is over the surface of the earth, where the differential surface area is dA . The second integral is over space, where $d\Omega$ is the differential solid angle. The other terms in these equations are as follows. The matrix \mathbf{G} is a 4×4 matrix of the antenna gain function. Each element in this matrix is a function of the look direction \mathbf{b} . For the first integral, \mathbf{b} is the unit vector pointing from the antenna to dA . For the second integral, \mathbf{b} is the unit vector in the direction specified by $d\Omega$.

The term $\Psi(\phi)$ is a rotation matrix defined by

$$\Psi(\phi) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 2\phi & -\sin 2\phi & 0 \\ 0 & \sin 2\phi & \cos 2\phi & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (6)$$

The rotation angle ϕ is the sum of the antenna polarization angle ϕ_{ant} and Faraday rotation angle ϕ_f due to the ionosphere: $\phi = \phi_{ant} + \phi_f$. The angle ϕ_{ant} is the angle between the antenna polarization vectors and the Earth polarization vectors. It is an implicit function of \mathbf{b} as well as the attitude of the Aquarius spacecraft. The Faraday rotation angle ϕ_f is a function of \mathbf{b} as well as the Earth's magnetic field vector \mathbf{B} and the electron density along the path \mathbf{b} .

$$\phi_f = \frac{1.35493 \times 10^{-5}}{\nu^2} N_e (-\mathbf{b} \cdot \mathbf{B}) \frac{\partial b}{\partial h} \quad (7)$$

where ν is frequency in GHz, N_e is vertically-integrated electron counts in TEC units, \mathbf{B} is the Earth's magnetic field vector in nanotesla units at the mean height of the ionosphere, and the last term is the partial derivative of slant range to the vertical height, which converts N_e from a vertically-integrated value to a slant-range integrated value. The rotation matrix is not required for the space integration because we assume the space radiation is unpolarized.

The ratio of the differential solid angle to the differential surface area is

$$\frac{\partial \Omega}{\partial A} = f_{lat} \frac{\cos \theta_i}{r^2} \quad (8)$$

where θ_i is the incidence angle and r is the range. For a spherical Earth, the leading term f_{lat} would be unity. However, the Earth is modeled as an oblate spheroid and as a consequence this term is a function of latitude, deviating about $\pm 1\%$ from unity.

The brightness temperature vector for Earth in equation (4) is

$$\mathbf{T}_{\mathbf{B},toa} = \begin{bmatrix} T_{BV,toa} + T_{BH,toa} \\ T_{BV,toa} - T_{BH,toa} \\ 0 \\ 0 \end{bmatrix} \quad (9)$$

where $T_{BV,toa}$ and $T_{BH,toa}$ are the v-pol and h-pol Earth brightness temperatures measured at the top of the atmosphere (TOA), but below the ionosphere. We have assumed that the 3rd and 4th Stokes parameters coming from the Earth are negligibly small at 1.4 GHz.

The brightness temperature vector for space is

$$\mathbf{T}_{\mathbf{B},space} = \begin{bmatrix} 2T_{Bspace} \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (10)$$

The space contribution consists of cosmic background radiation, galactic radiation, and radiation from the sun and the moon. We assume the space radiation is unpolarized (i.e., only the 1st Stokes is non-zero). (There may be a small 4th Stokes component, which needs to be investigated.). Section 2.2 discusses this space contribution in more detail.

The Earth's limb also contributes to the radiation received by the antenna. The Earth's limb varies from 260 K at the surface to 11 K at 10 km. Above 40 km, the limb brightness temperature is less than 0.001 K. When integrated over the antenna pattern, the limb contributes only 0.006 K to the 1st Stokes and is essentially zero for the 2nd through 4th Stokes.

At this point in our analysis, we drop the 4th Stokes from the notation. Aquarius does not measure the 4th Stokes, and it does not need to be considered. So hereafter, all \mathbf{T}_A and \mathbf{T}_B vectors now have just 3 components, and the antenna gain and rotation matrix are 3 by 3.

2.2 Radiation from Space

Space radiation consists of cosmic background (2.73 K), galactic, solar, and lunar components. This radiation is received by the antenna in two ways: directly and via Earth reflection and scattering. The contribution of direct lunar radiation is completely negligible (lunar radiation is a factor of 10^{-4} less than the solar radiation). However, lunar radiation reflecting off the ocean surface is not negligible because at certain times each month the reflected ray enters the antenna mainbeam.

These space radiation terms are denoted by:

1. Direct and reflected galactic radiation: \mathbf{T}_{A,gal_dir} and \mathbf{T}_{A,gal_ref}
2. Direct, reflected, and backscatter solar radiation: \mathbf{T}_{A,sun_dir} , \mathbf{T}_{A,sun_ref} , and \mathbf{T}_{A,sun_bak}
3. Reflected lunar radiation: $\mathbf{T}_{A,moon_ref}$

Because the solar radiation is so intense, one must consider both the specular reflected component that enters the far sidelobes of the antenna and the backscatter component that enters the mainbeam of the antenna.

Given these 6 terms, equations (4) and (5) can be partitioned as

$$\mathbf{T}_{A,earth} = \mathbf{T}_{A,earth_dir} + \mathbf{T}_{A,gal_ref} + \mathbf{T}_{A,sun_ref} + \mathbf{T}_{A,sun_bak} + \mathbf{T}_{A,moon_ref} \quad (11)$$

$$\mathbf{T}_{A,space} = \mathbf{T}_{A,gal_dir} + \mathbf{T}_{A,sun_dir} \quad (12)$$

where the new term $\mathbf{T}_{A,earth_dir}$ refers to radiation coming just from the earth (i.e., no space radiation reflections). It is better to directly compute the of antenna temperatures of the space reflections by numerically performing the required integrations rather than trying to model them as brightness temperature components reflected off the earth. For example, one could model the reflected galactic radiation as one component of $\mathbf{T}_{B,toa}$ in (4). However, the antenna pattern correction discussed in Section 3.3 works best for a smoothly varying brightness temperature scene. The galactic radiation field has very sharp features that would present a problem for the APC. Therefore, we decided to numerically compute the antenna temperatures for the various space reflections and store the results of the integrations as tables. The next subsections describe how the 6 space terms are computed.

2.2.1 Direct Galactic Radiation

The direct galactic radiation \mathbf{T}_{A,gal_dir} is computed by numerically evaluating the integral in (5),

$$\mathbf{T}_{A,gal_dir} = \frac{1}{4\pi} \int_{Space} \mathbf{G}(\mathbf{b}) \mathbf{T}_{B,gal} d\Omega \quad (13)$$

$$\mathbf{T}_{B,gal} = \begin{bmatrix} 2T_{Bgal} \\ 0 \\ 0 \end{bmatrix} \quad (14)$$

where T_{Bgal} comes from a galactic map [Le Vine and Abraham, 2004] that has the cosmic background radiation of 2.73K added in. The pixel size in the LeVine-Abraham map is

$0.25^0 \times 0.25^0$, and the minimum pixel value is about 3K. We interpret the 3 K floor of the galactic map as the cosmic background radiation (2.73 K) plus radiation coming from distant galaxies.

The computation of \mathbf{T}_{A,gal_dir} depends on the orbit position of the satellite and on the time of year as the Aquarius orbit precesses relative to the fixed galaxy every sidereal year (365.25636 days). A separate computation is done for each of the 3 radiometers because the antenna patterns are different. Tables of \mathbf{T}_{A,gal_dir} are generated for 1441 positions within an orbit (every $1/4^0$) and for 1441 periods during a sidereal year (about every 6 hours). These tables are specified by `tagal_dir_tab(1441,1441,3,3)`, where the 4 dimensions correspond to time of sidereal year, orbit position, Stokes number, and radiometer number. Time is referenced to January 1, 2010, 0Z, and orbit position is referenced to the South Pole node. The South Pole node is the point in the orbit where the polar component of spacecraft velocity vector changes from pointing south to pointing north. The orbit position is the angle between a vector pointing from the Earth center to the South Pole node and a vector pointing from the Earth's center to the current position of the satellite. For example, 90^0 would correspond approximately to the satellite crossing the equator going south to north. The periodicity of the time variable is one sidereal year (365.25636 days). Even though we are assuming the galactic T_B is unpolarized, antenna polarization mixing results in \mathbf{T}_{A,gal_dir} having all four Stokes components, although we drop the 4th Stokes. \mathbf{T}_{A,gal_dir} is a small (0.3K), slowly varying term and the granularity size of the table is more than sufficient. During operational processing a bi-linear interpolation is used to look up `tagal_dir_tab` as a function of orbit position and time of year.

The calculation of \mathbf{T}_{A,gal_dir} depends upon the assumed ascending equator crossing time for Aquarius. A value of 5:59:59.16 pm was used to generate the table `tagal_dir_tab`. If the actual ascending node time is different, the relative phase of the table can be adjusted via an input constant `orbit_phase_dif` that specifies the actual node time relative to 6:00:00 pm. Currently `orbit_phase_dif` is set to -0.84 seconds, and it will be revised after launch to the true value.

2.2.2 Reflected Galactic Radiation

The reflected galactic radiation \mathbf{T}_{A,gal_ref} is the most difficult space term to deal with. It can be large (5 K), have sharp features, and be modulated by the ocean surface roughness. To calculate \mathbf{T}_{A,gal_ref} , an integration over the Earth is done as follows

$$\mathbf{T}_{A,gal_ref} = \frac{1}{4\pi} \int_{Earth} \mathbf{G}(\mathbf{b}) \Psi(\phi) \mathbf{T}_{B,gal_ref} \frac{\partial \Omega}{\partial A} dA \quad (15)$$

where \mathbf{T}_{B,gal_ref} is the brightness temperature of the reflected galactic radiation at the top of the atmosphere and is given by

$$\mathbf{T}_{B,gal_ref} = \tau^2 (T_{Bgal} - T_{Bcos}) \mathbf{R} \quad (16)$$

$$\mathbf{R} = \begin{bmatrix} R_V + R_H \\ R_V - R_H \\ 0 \end{bmatrix} \quad (17)$$

where τ is the atmospheric transmittance and vector \mathbf{R} is the reflectivity for the 1st and 2nd Stokes in terms of the v-pol and h-pol reflectivity. Equation (16) shows that we subtract the

constant $T_{Bcos} = 3K$ from the LeVine-Abraham map before computing the reflected galaxy radiation. This is done because T_{Bcos} is the one and only space radiation term that is included in Earth radiation calculation (see Section 2.3). Hence, we must subtract it here to avoid including it twice.

Note that (16) only accounts for galactic reflections in the specular direction. In truth, bistatic scattering from a rough ocean will scatter galactic radiation from many different directions into the mainlobe of the antenna. In effect, a rough ocean surface tends to add additional spatial smoothing to \mathbf{T}_{A,gal_ref} . By neglecting this scattering effect we introduce a significant deficiency in the current forward model and retrieval algorithm. It is a complicated process that will be addressed between now and launch. The plan is to replace the current galactic reflection tables with new tables that include the scattering effect.

Tables of \mathbf{T}_{A,gal_ref} are made. As was the case for the direct galactic radiation, \mathbf{T}_{A,gal_ref} depends on the orbit position of the satellite and on the time of year. The tables have the same structure and format as the \mathbf{T}_{A,gal_dir} except that one additional dimension is included for wind speed. The tables have the form $\text{tagal_ref_tab}(1441,1441,3,3,5)$, where the first four dimensions are the same as described above for \mathbf{T}_{A,gal_dir} . The 5th dimension is wind speed going from 0 to 20 m/s in 5 m/s steps.

When computing $\text{tagal_ref_tab}(1441,1441,3,3,5)$, the atmospheric transmittance τ is set to unity and the reflectivities R_V and R_H are set to ocean reflectivity values corresponding to a surface temperature and salinity of 20°C and 35 psu, respectively, and wind speeds equaling 0, 5, 10, 15, and 20 m/s (i.e., the last dimension of the table). Also, the Faraday rotation angle is set to 0 when computing (15). During operational processing, an adjustment to the table values is made to convert these nominal values to the actual values corresponding to a given observation. This adjustment is now discussed.

During operational processing, NCEP and other ancillary data are used to determine the actual values for τ and R_V and R_H . Also, the Faraday rotation angle ϕ_f is computed as discussed in Section 3.4. The \mathbf{T}_{A,gal_ref} table values are adjusted to correspond to these actual values τ , R_V , R_H and ϕ_f as follows. First, the \mathbf{T}_{A,gal_ref} table values are converted to brightness temperatures using the APC equation (46) below. These classical Stokes T_{BS} are converted to conventional v-pol and h-pol T_B . Then the following adjustment is made:

$$T'_{BP,gal_ref} = \tau^2 \frac{R_p}{R_{0p}} T_{BP,gal_ref} \quad (18)$$

where the prime sign denotes the adjusted value and subscript p denotes polarization (V or H). The value τ is the NCEP transmittance, R_{0p} is the reflectivity computed at the nominal of 20°C and 35 psu, and R_p is the reflectivity computed at the NCEP temperature and reference salinity. T'_{BP,gal_ref} is then converted back to classical Stokes, Faraday rotation is applied, and the inverse APC equation (i.e. A^{-1}) is applied to convert back to antenna temperature. Simulations showed that there was less error in doing the adjustment at the T_B level as compared to simply applying the adjustment to the T_{AS} .

2.2.3 Direct Solar Radiation

The direct solar radiation \mathbf{T}_{A,sun_dir} is computed in the same way as for \mathbf{T}_{A,gal_dir} . However, the evaluation of the integral in (5) is much simpler because the sun is a very localized source and can be removed from the integral. Doing this gives

$$\mathbf{T}_{A,sun_dir} = T_{B,sun} \frac{\Omega_{sun}}{4\pi} \mathbf{G}(\mathbf{b}_{sun_direct}) \begin{bmatrix} 2 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (19)$$

where Ω_{sun} is the solid angle subtended by the sun and \mathbf{b}_{sun_direct} is the unit vector pointing from the spacecraft directly to the sun. The sun's brightness temperature is given by

$$T_{B,sun} = \frac{\lambda^2 F}{2k\Omega_{sun}} \quad (20)$$

where λ is the radiation wavelength, F is the solar flux, k is Boltzmann's constant, and Ω_{sun} is about $8.216\text{E-}5$ steradians. This assumes an angular radius of 0.293° , which is 10% greater than the optical angular radius [Wentz, 1978].

As with the direct galactic radiation, the computation of \mathbf{T}_{A,sun_dir} depends on the orbit position of the satellite and on the time of year. Tables of \mathbf{T}_{A,sun_dir} are generated in the same way as for \mathbf{T}_{A,gal_dir} and have the same structure and format, namely `tasun_dir_tab(1441,1441,3,3)`. That is to say, `tagal_dir_tab(1441,1441,3,3)` and `tasun_dir_tab(1441,1441,3,3)` are completely analogous with one exception. For the sun table, a change in the ascending node time cannot be simply handled by an orbit phase change. Rather the table will need to be regenerated after launch (a quick process that takes about an hour) when the true ascending node time is known.

In generating `tasun_dir_tab(1441,1441,3,3)`, we set the flux value F to 1 solar flux. Then for operational processing, the table values are multiplied by the actual flux value obtained from radio astronomy measurements. The solar flux F is a standard component of Aquarius ancillary data.

An analysis of the effect of solar radiation on Aquarius is given in Wentz [2005, 2007], which provides maps showing how the solar contamination varies during the course of a year. Typical values for \mathbf{T}_{A,sun_dir} are 0.05 K or less. However, because our knowledge error for antenna gain \mathbf{G} in the sun's direction may be large, the calculation of \mathbf{T}_{A,sun_dir} is subject to error. Post-launch analyses will be done to determine if \mathbf{T}_{A,sun_dir} is indeed small enough to neglect. The processing algorithm contains an option for setting \mathbf{T}_{A,sun_dir} to zero.

2.2.4 Reflected Solar Radiation

The reflected solar radiation \mathbf{T}_{A,sun_ref} comes from the specular reflection of sunlight from a location on the Earth far away from the observation cell. The reflected sunlight enters into the far sidelobes of the antenna. Even though the gain of these far sidelobes is very small, the intensity of the sun at 1.4 GHz is so large as to make this a potential problem. The reflected solar component can be found explicitly from the above formulation to be (also see Wentz [1978] and LeVine et al. [2005], Dinnat and Le Vine [2008])

$$\mathbf{T}_{A,sun_ref} = T_{B,sun} \frac{\Omega'_{sun}}{4\pi} \left\langle \tau^2 \mathbf{G}(\mathbf{b}) \Psi(\phi) \mathbf{R} \right\rangle_{ref} \quad (21)$$

where the prime sign on the sun solid angle Ω_{sun} indicates that the apparent solid angle of the sun reflecting off the spherical Earth is less than the solid angle when viewed directly. This effect is analogous to viewing an object through a convex mirror. The object will look smaller than it really is. This effect is discussed more in Section 2.2.6. The brackets in (21) denote an average over the neighborhood centered on the location of specular reflection, which is far removed from the observation footprint. The amount of averaging depends on surface roughness. For a specular (i.e., perfectly flat) surface, no averaging is required, and (21) can be evaluated for \mathbf{b} pointing in the direction of the specular reflection. For high winds when the surface becomes rough, the antenna gain needs to be averaged over 5° to 10° . In the sidelobe region, the terms τ^2 , $\Psi(\phi)$, and \mathbf{R} vary more slowly than $\mathbf{G}(\mathbf{b})$, and (21) can be approximated by

$$\mathbf{T}_{A,sun_ref} = T_{B,sun} \frac{\Omega'_{sun}}{4\pi} \tau_{ref}^2 \bar{\mathbf{G}}(\mathbf{b}) \Psi(\phi_{ref}) \mathbf{R}_{ref} \quad (22)$$

where the subscript *ref* denotes the quantity is calculated assuming a perfectly specular reflection and the overbar on the antenna gain function denotes that the antenna gain has been smoothed over an angular range to account for surface roughness.

The calculation of $R_{V,ref}$, $R_{H,ref}$, and τ_{ref} at the remote sun reflection point adds additional complexity to the modeling and algorithm. All of the ancillary data are keyed to the observation footprint which can be thousands of kilometers away from the sun reflection point. Furthermore, simulations [Wentz, 2005, 2007] indicate \mathbf{T}_{A,sun_ref} is very small, 0.01 K or less, and can probably be neglected. For now, we simply assume the reflectivity is that for a specular ocean surface at a temperature of 20°C and a salinity of 35 psu and the transmittance is set to unity. If post-launch analyses indicate \mathbf{T}_{A,sun_ref} has a measureable effect on the observations, then the antenna gain function $\mathbf{G}(\mathbf{b})$ will need to be revised (i.e., increased in the sidelobe region) and the retrieval algorithm will need to be modified to compute the reflectivity and atmospheric transmission at the remote location where the sun's specular reflection occurs.

Tables of \mathbf{T}_{A,sun_ref} are generated in the same way as for \mathbf{T}_{A,sun_dir} and have the same structure and format, namely `tasun_ref_tab(1441,1441,3,3)`. The processing algorithm contains an option for setting \mathbf{T}_{A,sun_refl} to zero.

2.2.5 Backscattered Solar Radiation

Most of the time, the Aquarius footprints will be entirely in the dark. However at the higher latitudes in the summer, the sun will be visible near the horizon, and solar radiation will impinge onto the Aquarius footprint at a grazing incidence angle. A very small portion of this sunlight will be backscattered into the mainlobe of the antenna. We denote this backscatter component as \mathbf{T}_{A,sun_bak} , and it has a magnitude on the order of 0.1 to 0.2 K when it does occur.

We use a model developed by *Dinnat and Le Vine* [2008] to specify \mathbf{T}_{A,sun_bak} . This model parameterizes \mathbf{T}_{A,sun_bak} in terms of the sun's zenith angle and wind speed. \mathbf{T}_{A,sun_bak} is tabularized as `tasun_bak_tab(161,26,3,3)`, where the 4 dimensions corresponds to sun zenith angle, wind speed, Stokes number, and radiometer number. The zenith angle goes from 58° to 90° in steps of 0.2° , and the wind speed goes from 0 to 25 m/s in steps of 1 m/s. This table was

generated assuming a solar flux F of 264 solar flux units. For operational processing, the values from `tasun_bak_tab(161,26,3,3)` are multiplied by $F/264$, where F is the actual flux value obtained from radio astronomy measurements.

The \mathbf{T}_{A,sun_bak} tables are computed assuming a nominal surface temperature and salinity of 20°C and 35 psu, an atmospheric transmittance of unit, and no Faraday rotation, i.e., the same nominal conditions used for the \mathbf{T}_{A,gal_ref} tables. During operational processing, an adjustment to the table values is made to convert these nominal values to the actual values corresponding to a given observation. This adjustment is exactly the same as described above for the reflected galactic radiation, i.e., equation (18). It should be pointed out that since \mathbf{T}_{A,sun_bak} is a very small term (0.1 to 0.2 K), the adjustment done by (18) has negligible effect over the ocean. The only appreciable effect of the adjustment is that over land the ratio R_P/R_{OP} becomes very small (land has a much smaller reflectivity than ocean), thereby reducing the value of \mathbf{T}_{A,sun_bak} , which is the correct thing to do.

2.2.6 Reflected Lunar Radiation

At certain times each month, moonlight reflected off the ocean surface enters the mainlobe of the antenna. This phenomenon is discussed by *Dinnat et al.* [2009] and is modeled here by using a simplified antenna gain function. A simplified approach can be used because the effect occurs rarely and is small in magnitude (1 K or less). The simplified gain pattern for the 1st and 2nd Stokes is

$$\tilde{\mathbf{G}} = \begin{pmatrix} G_{11} & G_{12} \\ G_{21} & G_{22} \end{pmatrix} 10^{-0.3 \left(\frac{\xi}{\xi_0} \right)^2} \quad (23)$$

where ξ is the angle between the antenna boresight vector and the vector from spacecraft to moon specular reflection point. The angle ξ_0 is the half-power angle of the antenna pattern. Its values for the inner, middle, and outer horns are 3.04°, 3.17°, and 3.24°. The values for the boresight gains G_{ij} are given in the computer code for each horn. Equation (23) is a very commonly used approximation for the gain over the mainlobe of the antenna. Given the small size of the effect, this approximation is perfectly adequate.

The reflected lunar radiation is then given by

$$\mathbf{T}_{A,mon_ref} = T_{B,moon} \frac{\Omega'_{moon}}{4\pi} \tau^2 \tilde{\mathbf{G}} \mathbf{R} \quad (24)$$

where the reflection vector \mathbf{R} is given by (17) but in this case the last component, which is zero, is discarded in order to match the 2x2 rank of $\tilde{\mathbf{G}}$. The terms \mathbf{R} and τ are computed from the ancillary data for the observation. $T_{B,moon}$ is assumed to be 275K and Ω'_{moon} is the apparent solid angle of the moon's reflection off the spherical earth. The relationship between the true solid angle Ω when viewed directly and the apparent solid angle Ω' when viewed as a reflection is

$$\Omega' = \frac{\Omega}{\left(1 + \frac{2s}{R_E} \right)^2} \quad (25)$$

where s is the slant path from the satellite to the point of reflection, and R_E is the Earth's radius. Ω' for the inner, middle, and outer horns is 3.93e-05, 3.79e-05, 3.63e-05 steradians. No adjustment is made for Faraday rotation, which is a small effect for the reflected lunar radiation.

2.3 Earth-Only T_B Equation

The one remaining term to be specified in the forward model is $T_{A,earth_dir}$, which is the radiation coming just from the earth (i.e., no space radiation either direct or reflected). The one exception, the uniform cosmic background radiation that reflects off the Earth, is included in $T_{A,earth_dir}$

$$T_{A,earth_dir} = \frac{1}{4\pi} \int_{Earth} \mathbf{G}(\mathbf{b}) \Psi(\phi) T_{BE} \frac{\partial \Omega}{\partial A} dA \quad (26)$$

where it is understood that T_{BE} refers to the TOA brightness temperature for radiation coming just from the earth. When doing forward modeling simulations, the integral in (26) is found by doing a very precise integration over the Earth's surface at a spatial resolution of about 1 km over the mainlobe of the antenna (a coarser resolution is used outside the mainlobe). This section discusses the Earth-only brightness temperature T_{BE} that appears in the kernel of the integral.

2.3.1 Theoretical Formulation

The AMSR-E ATBD [Wentz and Meissner, 2000] gives a very detailed description of the radiative transfer equation for T_{BE} . This formulation is also applicable to Aquarius. In this section, it is more convenient to work in terms of the modified Stokes parameters (i.e., v-pol and h-pol) rather than the classical Stokes parameters. We are assuming that at 1.4 GHz, T_{BE} 3rd and 4th Stokes are zero. The v-pol and h-pol components of T_{BE} are given by

$$T_{BE,P} = T_{BU} + \tau [E_P T_S + T_{BP\Omega}] \quad (27)$$

where subscript P denotes polarization, either V or H . T_{BU} is the brightness temperature of the upwelling atmospheric radiation, τ is the atmospheric transmittance, E_P is the Earth surface emissivity, T_S is the Earth surface temperature (K), and $T_{BP\Omega}$ is the downwelling sky radiation that is scattered off the Earth surface in the direction of the observation.

The atmospheric terms can be expressed in terms of the transmittance function $\tau(s_1, s_2)$

$$\tau(s_1, s_2) = \exp \left(- \int_{s_1}^{s_2} ds \alpha(s) \right) \quad (28)$$

which is the transmittance between points s_1 and s_2 along the propagation path s . The term $\alpha(s)$ is the atmosphere absorption due to oxygen, water vapor, and liquid water. See Wentz and Meissner [2000] for a more complete description of $\alpha(s)$. The total transmittance τ in (27) is given by

$$\tau = \tau(0, S) \quad (29)$$

where S is the slant range from the surface to the top of the atmosphere. The upwelling and downwelling atmosphere emissions are given by

$$T_{BU} = \int_0^S ds \alpha(s) T(s) \tau(s, S) \quad (30)$$

$$T_{BD} = \int_0^S ds \alpha(s) T(s) \tau(0, s) \quad (31)$$

where $T(s)$ is the air temperature profile. The scattering integral for the downwelling radiation is

$$T_{BP\Omega} = \frac{\sec \theta_i}{4\pi} \int_0^{\pi/2} \sin \theta_s d\theta_s \int_0^{2\pi} d\varphi_s (T_{BD} + \tau T_{B\cos}) [\sigma_{o,c}(\mathbf{k}_s, \mathbf{k}_i) + \sigma_{o,\times}(\mathbf{k}_s, \mathbf{k}_i)] \quad (32)$$

where θ_s is the zenith angle for the downwelling radiation impinging on the surface, and θ_i is the incidence angle for the upwelling radiation leaving the surface in the direction of the observation. The integral is over the 2π steradians of the upper hemisphere. The term $\sigma_{o,c}$ and $\sigma_{o,\times}$ are the co-pol (i.e. polarization equal P) and cross-pol (i.e. polarization orthogonal to P) bistatic normalized cross sections, which are functions of unit propagation vectors \mathbf{k}_i and \mathbf{k}_s that denote the direction of the upwelling and downwelling radiation, respectively. The angle φ_s is the azimuth of \mathbf{k}_s relative to \mathbf{k}_i . These cross sections specify what fraction of power coming from \mathbf{k}_s is scattered into \mathbf{k}_i . T_{BD} is the brightness temperature of the downwelling atmospheric radiation, and $T_{B\cos}$ is the cosmic background plus distant galaxies radiation and equals 3 K (see Section 2.2.2).

The surface reflectivity is given by an equation similar to (32):

$$R_p = \frac{\sec \theta_i}{4\pi} \int_0^{\pi/2} \sin \theta_s d\theta_s \int_0^{2\pi} d\varphi_s [\sigma_{o,c}(\mathbf{k}_s, \mathbf{k}_i) + \sigma_{o,\times}(\mathbf{k}_s, \mathbf{k}_i)] \quad (33)$$

The surface emissivity E_p is given by Kirchhoff's law to be

$$E_p = 1 - R_p \quad (34)$$

To numerically compute \mathbf{T}_{BE} from the above theoretical equations, a number of empirical models are used as is described in the next sections.

2.3.2 Empirical Approach to Specifying Atmospheric Terms

The atmospheric terms are the upwelling and downwelling brightness temperatures T_{BU} and T_{BD} , and the atmospheric transmittance τ . These are computed by numerically integrating equations (28) through (31). For operational processing, we use NCEP profiles of pressure, temperature, humidity, and liquid water to find profiles of $\alpha(s)$. The NCEP profiles are interpolated to the exact time and location of the Aquarius observations. For the oxygen absorption component of $\alpha(s)$ we use the expressions given by *Liebe et al.* [1992]. For the water vapor absorption component of $\alpha(s)$ we use the expressions given by *Rosenkranz* [1998]. We make small modifications to both the Liebe and Rozenkranz formulations based on many years of analyzing satellite microwave observations. At 1.4 GHz, the only modification of any importance is the non-resonance continuum temperature coefficient which was changed from

Liebe's exponent value of 0.8 to 1.5. This change was based on an analysis of WindSat and AMSR-E 7 GHz brightness temperatures. A paper on this is planned for 2011.

2.3.3 Empirical Approach to Specifying Emissivity

The theoretical modeling of the bistatic normalized cross sections is not sufficiently advanced to provide sufficiently accurate estimates of R_p and E_p . Instead, we use the conventional approach of expressing the emissivity E_p in terms of a specular component (i.e. flat surface) and a wind-induced component:

$$E_p = E_{0p} + \Delta E_p(W, \phi_r) \quad (35)$$

where relative wind direction ϕ_r is the direction of the wind relative to the azimuth angle of the Aquarius look direction. The specular component E_{0p} is computed using the dielectric constant model of *Meissner and Wentz* [2004]. For the wind-induced component, we use an empirical model derived from L-band aircraft measurements [*Yueh et al.*, 2010]. Yueh expresses his results in terms of an increase in brightness temperature with wind speed:

$$\begin{aligned} \Delta T_{BV}(W) &= (0.275 - 0.0024153 \theta_i + 1.4026 \cdot 10^{-4} \theta_i^2 - 2.3326 \cdot 10^{-6} \theta_i^3) W \\ \Delta T_{BH}(W) &= (0.275 + 0.0030010 \theta_i - 2.5181 \cdot 10^{-6} \theta_i^2 - 6.9763 \cdot 10^{-7} \theta_i^3) W \end{aligned} \quad (36)$$

where θ_i is the Earth incidence angle (deg) and W is the 10-m wind speed (m/s). We convert this to a change in emissivity as follows:

$$\Delta E_p(W, \phi_r) = \frac{\Delta T_{BP}(W)}{276.16} \frac{E_{0p}(T_s, S)}{E_{0p}(276.16, 35)} + \Phi(W, \phi_r) \quad (37)$$

where the first term is the isotropic wind-induced emissivity and the second term accounts for the wind direction variation. Yueh's measurements were done in cold water around 3°C, and hence to convert to emissivity one must divide by 276.16 K. Furthermore, to convert to the actual water temperature and salinity of the Aquarius observation, we multiply by the ratio of the actual specular emissivity to the specular emissivity corresponding to Yueh's measurements. We assume a nominal salinity of 35 psu for Yueh's measurements, although this choice has very little effect on the calculation.

The wind direction term for ΔE_p is small and is yet to be specified. As a placeholder, we are assuming the following form for the wind-direction dependence.

$$\Phi(W, \phi_r) = [(p_{1p} + p_{2p}\theta_i)\cos\phi_r + (p_{3p} + p_{4p}\theta_i)\cos 2\phi_r]W \quad (38)$$

where the p coefficients are currently set to zero. When the Aquarius Science Team has come to agreement on the specification of this term, the p coefficients will be updated.

For operational processing, the surface temperature T_s is currently the NCEP daily, 0.25° product and the wind speed W and direction ϕ_r are the NCEP 6-hour, 1° product.

2.3.4 Empirical Approach to Specifying Reflected and Scattered Radiation

The remaining term that needs to be specified is the scattering integral for the downwelling radiation: $T_{BP\Omega}$. A primary reason for computing the space radiation terms separately, as

described in Section 2.2, is to facilitate the computation of $T_{BP\Omega}$. In the absence of sharply varying space terms, the integral now just contains $T_{BD} + \tau T_{B\cos}$, a small term that varies very slowly over angle. The bistatic cross section has a sharp peak in the specular direction at which $\theta_i = \theta_s$ and $\varphi_s = 180^\circ$, and over this sharp peak $T_{BD} + \tau T_{B\cos}$ varies little and can be removed from the integral. The remaining integral is simply the surface reflectivity, and hence one has

$$T_{BP\Omega} = (T_{BD} + \tau T_{B\cos}) R_P \quad (39)$$

where T_{BD} and τ conveniently have the same slant path angle as T_{BU} .

2.3.5 Empirical Approach to Handling Land and Sea-Ice Observations

Although our primary focus is observations over the ocean, the formulation we have presented applies equally well to land and sea-ice observations. The only exception is that the sea-surface emissivity E_P given by (37) needs to be replaced by a land or sea-ice emissivity, with Kirchhoff's law then giving R_P . For observation of mixed surfaces, the following expressions are used

$$R_P = f_{\text{water}} R_{P\text{water}} + f_{\text{land}} R_{P\text{land}} + f_{\text{ice}} R_{P\text{ice}} \quad (40)$$

$$E_P T_s = (1 - R_{P\text{water}}) T_{\text{water}} + (1 - R_{P\text{land}}) T_{\text{land}} + (1 - R_{P\text{ice}}) T_{\text{ice}} \quad (41)$$

where f denotes fractional area and T denotes surface temperature. Equations (40) and (41) are then substituted into (27). The fractional land f_{land} is computed from the number of $1/12^\circ$ land pixels that are within an observation footprint and this calculation is based on a static land mask. The fractional sea-ice f_{ice} comes from the NCEP operational sea-ice dataset. The fractional water is then $f_{\text{water}} = 1 - f_{\text{land}} - f_{\text{ice}}$. The reflectivities for land and sea ice are discussed in Appendix A.

3 Salinity Retrieval Algorithm

The salinity retrieval algorithm consists of a number of steps that are intended to remove the unwanted sources of radiation (galaxy, sun, moon, and Earth's atmosphere) in order to obtain just the Earth's surface emission term. A simple regression is then use to estimate salinity from the surface emission. These steps include:

1. The radiation received from the galaxy, sun, and moon is subtracted from the T_A measurements.
2. An antenna pattern correction (APC) is done that removes cross-polarization contamination and corrects for sidelobes. The APC converts the top-of-the-ionosphere (TOI) antenna temperature to a brightness temperature.
3. Faraday rotation is removed using the 3rd Stokes T_B measurement. This provides the top-of-the-atmosphere (TOA) brightness temperature.
4. The atmospheric components of the TOA T_B are computed using NCEP operational fields and are then removed from the TOA T_B . This provides the surface emission by itself.
5. The salinity value is retrieved from the surface emission using a simple least-squares regression.

Each of these steps is now described.

3.1 Removal of the Radiation Coming from Space

The first step in salinity retrieval is to remove the contribution of space radiation from the antenna temperature measurement $\mathbf{T}_{A,mea}$. Section 2.2 lists the 6 components of space radiation and describes how they are computed during operational processing. This subtraction is represented by

$$\mathbf{T}_{A,earth_dir} = \mathbf{T}_{A,mea} - \mathbf{T}_{A,gal_dir} - \mathbf{T}_{A,gal_ref} - \mathbf{T}_{A,sun_dir} - \mathbf{T}_{A,sun_ref} - \mathbf{T}_{A,sun_bak} - \mathbf{T}_{A,mon_ref} \quad (42)$$

where we are now just left with the radiation coming directly from the Earth.

3.2 Definition of Reference Brightness Temperature

At this point in describing the retrieval algorithm, we need to define the reference brightness temperature that we are seeking to retrieve from $\mathbf{T}_{A,earth_dir}$. One possible choice is the Earth TOA T_B at boresight. However, we think a better choice is to define the reference brightness temperature as an average over the 3-dB Aquarius footprint since this is closer to what is actually measured. To be precise, the reference TOA T_B is defined as

$$\bar{\mathbf{T}}_{BE,toa} = \frac{\int_{3dB \text{ footprint}} \mathbf{T}_{BE,toa}(\bar{\theta}_i) dA}{\int_{3dB \text{ footprint}} dA} \quad (43)$$

where the integral is over the 3-dB footprint and the overbar denotes the average over the footprint. The 3-dB footprint is defined as that part of the Earth integral for which the angle between the boresight vector \mathbf{b}_0 and the look vector \mathbf{b} is less than 3.07° , 3.17° , and 3.24° for the inner, middle, and outer horns, respectively. We further specify that when doing the footprint averaging, the incidence angle is held to a constant value $\bar{\theta}_i$, which is the gain-weighted average incidence angle given by

$$\bar{\theta}_i = \chi \theta_{i,boresight} \quad (44)$$

where $\theta_{i,boresight}$ is the boresight incidence angle, and χ is 1.00177, 1.00186, 1.00148 for the inner, middle, and outer horns, respectively. This adjustment is so small that it probably is not needed and one could simply use the boresight incidence angle for $\bar{\theta}_i$. Thus by definition $\bar{\mathbf{T}}_{BE,toa}$ is only a function of the Earth scene being viewed, with all antenna pattern effects removed.

The top-of-the-ionosphere (TOI) reference brightness temperature is denoted by $\bar{\mathbf{T}}_{BE,toi}$ and is given by applying Faraday rotation:

$$\bar{\mathbf{T}}_{BE,toi} = \Psi(\phi_f) \bar{\mathbf{T}}_{BE,toa} \quad (45)$$

3.3 Estimation of Top-of-the-Ionosphere Brightness Temperature

Now that we have defined our reference T_B , we must estimate its value given the antenna temperature $T_{A,earth_dir}$. In principle we are seeking the solution of the integral equation given by (26): given $T_{A,earth_dir}$ what is $\bar{T}_{BE,toi}$? It is not possible to directly invert the integral, and other means are required. We use the following method.

Forward simulations are performed for which a year of simulated $T_{A,earth_dir}$ are generated. This represents about 25 million observations for each horn at intervals of 1.44 seconds. The following regression is then assumed.

$$\hat{T}_{BE,toi} = \mathbf{A} \cdot T_{A,earth_dir} \quad (46)$$

where \mathbf{A} is a 3 by 3 matrix and is called the antenna pattern correction (APC) matrix and the ‘hat’ on $T_{BE,toi}$ denotes that this is an estimated quantity as compared to the true value. In addition to providing $T_{A,earth_dir}$, the simulation also provides the true value of $\bar{T}_{BE,toi}$. The standard least-squares method is used to find the APC matrix \mathbf{A} that minimizes the variance of $\hat{T}_{BE,toi} - \bar{T}_{BE,toi}$.

When deriving the APC matrix \mathbf{A} , we excluded simulated observations that contain sea ice or that are a mixture of land and water. That is to say, regression (46) is only done for observations that are totally land or totally water, i.e., uniform scenes. We did not think it was a good idea to train the regression with extremely non-uniform scenes, which pose many difficulties when trying to relate antenna temperatures to brightness temperatures.

Considering all complexities of the integral equation (26), it is not obvious if a simple regression like (46) will perform adequately. To evaluate its performance, we compute the rms value of $\hat{T}_{BE,toi} - \bar{T}_{BE,toi}$ averaged over all the simulated observations. These statistics were done separately for all-ocean and all-land observations, but the same APC matrix was used for both. Over the ocean, the rms v-pol and h-pol values ranged from 0.05 to 0.08 K. Over land, the rms values were considerably higher, ranging from 1 to 2 K. The higher land values are due to the land T_B having more variability. A small number of land observations having very large variability show errors of 10-20 K, which have a great influence on the rms statistics. These results show that the APC regression (46) works well for uniform scenes, like the ocean. Non-uniform scenes present a problem for the APC, which is probably unavoidable.

We experimented with deriving the APC just with ocean observations since this is our primary focus. There was a slight improvement when the ocean-only APC was applied to the ocean observations, but the improvement was very small compared to the overall 0.05 to 0.08 K performance, and we elected to stay with the ocean+land APC, which is trained over the full range of T_A .

The largest error in the APC is with respect to the 3rd Stokes for the outer horn, for which the ocean-only observations exhibit an rms of 0.2K. However, the 3rd Stokes is just used for Faraday rotation correction, and the mapping of this error into the top-of-the-atmosphere (TOA) T_B is very small.

The 0.05 to 0.08 K performance of the APC is of some concern, given the demanding requirements for Aquarius brightness temperature accuracy. We did some experiments in an

attempt to improve its performance, such as using an ocean-only APC, using separate APC for ascending and descending orbit segments, and adding higher order terms to (46). These attempts helped slightly, but not enough to warrant their implementation. However, with more time and analysis, we do think that there is the potential for improving the APC performance.

3.4 Correction for Faraday Rotation

The next step in the retrieval is a correction for Faraday rotation. *Yueh* [2000] gave a detailed description of the Faraday rotation problem and proposed measuring the 3rd Stokes parameter to remove its effect, as we will now discuss. Faraday rotation is removed by applying the following expression.

$$\hat{\mathbf{T}}_{\text{BE},\text{toa}} = \Psi(-\phi_f) \hat{\mathbf{T}}_{\text{BE},\text{toi}} \quad (47)$$

If one assumes that the 3rd and 4th TOA Stokes from the Earth are negligibly small, one may set the $\bar{\mathbf{T}}_{\text{BE},\text{toa}}$ 3rd Stokes to zero and obtain the Faraday rotation angle:

$$\phi_f = \frac{1}{2} \arctan \left(\frac{\hat{T}_{\text{BE},\text{toi},3}}{\hat{T}_{\text{BE},\text{toi},2}} \right) \quad (48)$$

where the last subscript denotes Stokes number. Substituting (48) into (47) one obtains the TOA \mathbf{T}_B

$$\begin{aligned} \hat{T}_{\text{BE},\text{toa},1} &= \hat{T}_{\text{BE},\text{toi},1} \\ \hat{T}_{\text{BE},\text{toa},2} &= \sqrt{\left[\hat{T}_{\text{BE},\text{toi},2} \right]^2 + \left[\hat{T}_{\text{BE},\text{toi},3} \right]^2} \end{aligned} \quad (49)$$

Wentz [2006] analyzed the error between the estimated $\hat{\mathbf{T}}_{\text{BE},\text{toa}}$ and the true $\bar{\mathbf{T}}_{\text{BE},\text{toa}}$. The rms difference was about 0.04 K for ocean v-pol and h-pol observations. The *Wentz* [2006] results used an antenna gain pattern based on a JPL computer model. Since then, the computer model antenna pattern has been replaced by the scale-model antenna pattern, which has considerably larger cross-polarization terms. These large cross-polarization terms result in larger error when doing the APC. The $\hat{\mathbf{T}}_{\text{BE},\text{toa}} - \bar{\mathbf{T}}_{\text{BE},\text{toa}}$ rms value is now 0.05 to 0.08 K, nearly all of which is due to the APC error as mentioned in the previous section.

3.5 Removal of Atmospheric Effects

In this subsection we switch over to using the modified Stokes parameters (v-pol and h-pol) rather than the classical Stokes parameters for $\hat{\mathbf{T}}_{\text{BE},\text{toa}}$, and these two components are denoted simply as $T_{\text{BE},P}$, where subscript P denotes polarization (either V or H). This step in the retrieval algorithm is intended to remove the effect of the atmosphere. This is done by inverting (27) to yield surface emission $T_{\text{BE},\text{sur}}$.

$$T_{\text{BE},P,\text{sur}} \equiv E_P T_S = \frac{T_{\text{BE},P} - T_{\text{BU}}}{\tau} - T_{\text{BP}\Omega} \quad (50)$$

Substituting (39) in (50) gives

$$T_{BE,P,sur} \equiv E_P T_S = \frac{T_{BE,P} - T_{BU}}{\tau} - (T_{BD} + \tau T_{Bcos}) R_P \quad (51)$$

Noting that $R_P = 1 - E_P$, (51) can be rewritten as

$$T_{BE,P,sur} = \left[\frac{\frac{T_{BE,P} - T_{BU}}{\tau} - (T_{BD} + \tau T_{Bcos})}{T_S + (T_{BD} + \tau T_{Bcos})} \right] T_S \quad (52)$$

where the bracketed term is the surface emissivity.

The atmospheric terms for the upwelling and downwelling brightness temperature T_{BU} and T_{BD} , and the atmospheric transmittance τ are computed by numerically integrating equations (28) through (31). For operational processing, we use NCEP profiles of pressure, temperature, humidity, and liquid water to find profiles of $\alpha(s)$. The NCEP profiles are interpolated to the exact time and location of the Aquarius observations. See Section 2.3.2 for more details. The surface temperature T_S currently comes from the NCEP daily, 0.25° product. After launch, other sources for T_S will be considered such as AMSR-E and WindSat microwave-only retrieval of sea surface temperature. T_{Bcos} is a constant 3 K. Given these ancillary data, (52) can be calculated to yield the surface emission brightness temperature. Note that this calculation of $T_{BE,P,sur}$ is done for all surface types (ocean, land, sea-ice, and mixed).

3.6 Estimation of Salinity Given Surface Emission Brightness Temperature

Over the ocean, the surface emission $T_{BE,P,sur}$ depends on surface temperature T_S , surface salinity S , surface roughness, and Earth incidence angle θ_i . For now, we are parameterizing the surface roughness effect simply as a function of the wind measured 10 meters above the surface, where W denotes the speed (m/s) and ϕ_r denotes the relative wind direction. The wind direction effect given by (38) is first removed from the surface T_B .

$$T'_{BE,P,sur} = T_{BE,P,sur} - \Phi(W, \phi_r) T_S \quad (53)$$

where the prime sign denotes that the wind direction effect is removed.

Wentz and Yueh [2004] described the algorithm for estimating sea-surface salinity from the surface emission $T'_{BE,P,sur}$. The algorithm takes the form

$$S = s_0(\theta_i, t_S) + s_1(\theta_i, t_S) T'_{BE,V,sur} + s_2(\theta_i, t_S) T'_{BE,H,sur} + s_3(\theta_i, t_S) W \quad (54)$$

where θ_i is the incidence angle, t_S is the sea-surface temperature in $^\circ\text{C}$ ($T_S = t_S + 273.15$), and W is sea-surface wind speed (m/s). The s coefficients are functions of θ_i and t_S and are in tabular form. The algorithm is trained by deriving a set of s coefficients that minimize variance between the salinity S given by (54) and the true salinity. Separate sets of s coefficients are found for 251 incidence angles going from 25° to 50° in 0.1° steps and 451 t_S values going from -5°C to 40°C in 0.1°C steps. These 251×451 tables are interpolated to the specified value for θ_i and t_S .

The algorithm training requires that $T'_{BE,P,sur}$ be computed over the full range of S , T_S , W and θ_l using equations (35) through (38). Note that this is the only point in the retrieval algorithm where the specification of the dielectric constant of sea water [Meissner and Wentz, 2004], and the wind-induced emissivity [Yueh *et al.*, 2010] comes into play. Using a different dielectric model or a different wind model would result in a different set of s coefficients.

For a given θ_l and t_S , the relationship between surface brightness temperature and salinity is close to linear, but not quite. If necessary, we will supplement equation (54) by adding a second stage algorithm that will remove any error caused by the deviation from linearity. This type of two-stage algorithm has proven very effective in handling the non-linearity characteristic in the AMSR-E retrievals. However, any such fine tuning should wait until the L-band wind model (i.e., equations 36-38) is known more precisely. We expect that about 6-months after launch an improved wind model will be developed, and we can then take a closer look equation (54).

Note that in training the algorithm, a different amount of noise can be applied to the v-pol and h-pol T_B to account for the actual error in these T_B retrievals. Also, an analogous algorithm can be developed that uses the sum of v-pol and h-pol T_B to eliminate residual Faraday rotation error. The salinity retrievals from the V+H algorithm can be compared to those coming from the dual-polarization algorithm to test if there is any residual Faraday rotation error. This type of experimenting will be done after launch.

Another alternative to (54) is to subtract the wind-induced T_B correction $\Delta T_{BP}(W)$ from $T_{BE,P,sur}$ prior to the salinity retrieval. This is the approach used for the algorithm derived during the WISE experiments [Camps *et al.*, 2002]. However as said above, it is probably best to wait until we have the improved post-launch wind model before trying these different alternatives.

The salinity retrieval is very sensitive to errors in T_S and W . The pre-launch version of the algorithm currently uses the NCEP daily, 0.25° product for T_S and the NCEP 6-hour, 1° product for W . After launch, other sources for T_S and W will be considered. Microwave retrievals of sea surface temperature from AMSR-E and WindSat could possibly prove to be more accurate than the NCEP sea surface temperatures. Also, at some point, we expect to start using the wind speed derived from the Aquarius microwave scatterometer.

3.7 Correction for Land Entering the Antenna Sidelobes

One option that is being evaluated is the removal of sidelobe contamination when the Aquarius observation is close to land. Simulations have shown that the salinity retrieval degrades quickly as the footprint approaches land (closer than 400 km). This land-contamination error, which is shown in the Wentz [2006] study, is defined as

$$\Delta \mathbf{T}_{BE,toa} = \hat{\mathbf{T}}_{BE,toa} - \bar{\mathbf{T}}_{BE,toa} \quad (55)$$

which is the difference of the estimated TOA T_B minus the true TOA T_B coming from the simulation. We plan to use the Aquarius simulator to produce tables of $\Delta \mathbf{T}_{BE,toa}$. These tables will be stratified according to latitude (0.25° increment), longitude (0.25° increment), ascending/descending (1 or 2), month (12), horn (3), and polarization (2). The monthly variable is required to account for seasonal variability in the land brightness temperatures and the variability of sea ice. (Sea ice will be particularly challenging due to interannual variability.)

The land-correction tables will have the form $T_{b_land_correction}(1440,720,2,12,3,2)$. In principle these table values could be subtracted from the estimated TOA T_B in order to remove the land contamination. Possibly, this might provide usable salinity retrievals closer to land: maybe to within 200 km of land.

Other methods for the removal on land contamination are also being investigated. One method for sidelobe removal that has been applied to radiometers on JASON and ENVISAT is to divide the integration (e.g. in equation 26) into additional sectors such as the on-Earth sidelobes to obtain a mainbeam brightness temperature, and to eventually deconvolve the mainbeam brightness temperature [Brown, 2005].

4 Remaining Work before Launch

The biggest challenge we face before launch is improving our modeling of the reflected galactic radiation (Section 2.2.2). Currently, we are only accounting for galactic reflections in the specular direction. In truth, bistatic scattering from a rough ocean will scatter galactic radiation from many different directions into the mainlobe of the antenna. Between now and launch, we plan to include bistatic scattering in our simulator. This is a formidable undertaking because it means putting a double integral into the kernel of the T_A integral equation (4). However, we have done some initial testing, and the problem is tractable although the processing time is considerable. We estimate it will take 32 processors about 2 months to do the necessary calculations. No changes to the salinity retrieval algorithm will be required other than updating the galactic reflection tables $tagal_ref_tab(1441,1441,3,3,5)$. These tables have already been parameterized in term of wind speed in anticipation of this update.

Another issue that needs revolving before launch is the specification of the wind directional term for $\Phi(W, \phi_r)$ given by (38). Again this should not require changes to the retrieval algorithm other than specifying the p coefficients, which are currently set to zero.

Finally, we want to implement the land correction tables discussed in Section 3.7. Whether this is done before or after launch needs to be decided. This change will require a small addition to the current code.

Finally, research is underway at the George Washington University and at the Polytechnic University of Catalonia to refine the *Klein and Swift* [1977] model function for emissivity at L-band that relates the brightness temperature to sea surface temperature and salinity. After launch, the salinity retrievals using the Meissner-Wentz dielectric constant model can be compared with those using the alternative dielectric constant model. This type of experimenting is done by recomputing the s coefficients in (54) using a different dielectric constant model. Similar experimenting can be done with different wind-induced emissivity models.

5 References

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6 Appendix A. Land and Sea-Ice Reflectivities

This appendix will be done soon. It will contain expressions for computing the reflectivity of land and sea ice.